New faithfulness-Centric Interpretability Paradigms for Natural Language Processing

Andreas Madsen





New Interpretability Paradigms

2. Faithfulness Measure Models

Outline

1. Background on Interpretability

3. Self-explanations



"The ability to explain or present (a model or dataset) in understandable terms to a human."

Doshi-Velez, F., & Kim, B (2017). Towards A Rigorous Science of Interpretable Machine Learning.

Interpretability



Identify model issues

Only people with a CS degree are qualified typists [1].

[1] Fuller, J. (2021). Companies Need More Workers. Why Do They Reject Millions of Résumés? The Project on Workforce.



Identify actionable fixes

Prediction Model Ē

Scientific discovery



Sentiment Classification





Importance Measures





Post-hoc Interpretability for Neural NLP: A Survey

ANDREAS MADSEN^{*}, SIVA REDDY^{†‡}, and SARATH CHANDAR^{*§}, Mila, Canada

Neural networks for NLP are becoming increasingly complex and widespread, and there is a growing concern if these models are responsible to use. Explaining models helps to address the safety and ethical concerns and is essential for accountability. Interpretability serves to provide these explanations in terms that are understandable to humans. Additionally, post-hoc methods provide explanations after a model is learned and are generally model-agnostic. This survey provides a categorization of how recent post-hoc interpretability methods communicate explanations to humans, it discusses each method in-depth, and how they are validated, as the latter is often a common concern.

CCS Concepts: • Computing methodologies → Natural language processing; Neural networks.

Additional Key Words and Phrases: Interpretability, Transparency, Post-hoc explanations.

ACKNOWLEDGMENTS

SC and SR are supported by the Canada CIFAR AI Chairs program and the NSERC Discovery Grant.

1 INTRODUCTION

Large neural NLP models, most notably BERT-like models [20, 36, 70], have become highly widespread, both in research and industry applications [134]. This increase of model complexity is motivated by a general correlation between model size and test performance [20, 56]. Due to their dere black-box models. A growing concern immense complexity, these models are ge is therefore if it is responsible to depl

Concerns such as safety, ethics, and accountebility are particularly important when machine learning is used for high-stakes decisions, such as healthcare, criminal justice, finance, etc. [102], NLP-focused applications such as translation, dialog systems, resume screening, search, includi

an "incompleteness in the problem formalization". While these issues can be partially prevented with robustness and fairness metrics, it is often to ot possible to consider all failure modes. Therefore, igh model explanations. Furthermore, when models do ist be provided to facilitate the accountability process. quality assessment should also be done fail in critical applications, explanations m Providing these explanations is often a core motivation for interpretability. In Section 2 we provide aditional motivating factors.

Doshi-Velez and Kim [37] define *interpretability* as the "ability to explain or to present in understandable terms to a human". However, what constitutes as an "understandable" explanation is an interdisciplinary question. An important work from social science by Miller [79], argues that effective explanations must be selective in the sense one must select "one or two causes from a sometimes infinite number of causes". Such observation necessitates organizing interpretability methods by how and what they selectively communicate.

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lower

abstraction

higher

abstraction

	less information mo						
	post-hoc					intrinsic	
	black-box	dataset	gradient	embeddings	white-box	model sp	
local explanation							
input features	Occlusion -based $\S2.5.2$		Gradient -based $\S2.5.1$			Attent -based §	
adversarial examples	$SEA^{\mathcal{M}}$ § A.1.2		$\operatorname{HotFlip}$	p §A.1.1			
$ \begin{array}{c} \text{influential} \\ \text{examples} \end{array} $		Influence Functions ^{\mathcal{H}} § A.2.1 TracIn ^{\mathcal{C}} § A.2.3		Representer Poin	Prototy Networ		
counter- factuals	$\begin{array}{c} \text{Polyjuice}^{\mathcal{M},\mathcal{D}} \\ \$ 2.6.1 \end{array}$	$MiCE^{\mathcal{M}}$ §2.6.2					
natural language	predict-then- explain $^{\mathcal{M}}$ § 2.7.2					$\begin{array}{c} \text{explain-t} \\ \text{predict}^{\mathcal{M}} \end{array}$	
class explanation							
concepts					$\operatorname{NIE}^{\mathcal{D}}$ §A.3.1		
global explanation							
vocabulary				Project §A.4.1, Rotate §A.4.2			
ensemble	SP-LIMI	E § A.5.1					
linguistic information	$\begin{array}{c} \text{Behavioral} \\ \text{Probes}^{\mathcal{D}} \ \S \text{A.6.1} \end{array}$			Structural $\operatorname{Probes}^{\mathcal{D}} \S A.6.2$	Structural Probes ^{\mathcal{D}} §A.6.2	Auxilia Task ²	
rules	$\operatorname{SEAR}^{\mathcal{M}}$	§A.7.1 Compo	sitional Explana	tions of Neurons [†]	A.7.2		











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Post-hoc Interpretability for Neural NLP: A Survey

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Leave one out (LOO)





Leave one out (LOO)











Attention

Positive sentiment









Attention

Disagreement problem





faithfulness ^[1]

"How accurately it (the explanation) reflects the true reasoning process of the model."

[1] Jacovi, A., & Goldberg, Y. (2020). Towards Faithfully Interpretable NLP Systems: How Should We Define and Evaluate Faithfulness? ACL 2020

Desirables

human-groundedness^[2]

How useful is the explanation to humans.

[2] Doshi-Velez, F., & Kim, B (2017). Towards A Rigorous Science of Interpretable Machine Learning.



Human-groundedness

Counterfactual generation



Ross, A., Marasović, A., & Peters, M. (2021). Explaining NLP Models via Minimal Contrastive Editing (MiCE). Findings of the Association for Computational Linguistics: ACL-IJCNLP 2021

Contrastive explanations

Input: *Can you stop the dog from* **Output:** barking

1. Why did the model predict "barking"? Can you stop the dog from

2. Why did the model predict "barking" *instead of* "crying"? Can you stop the dog from

3. Why did the model predict "barking" *instead of* "walking"? Can you stop the dog from

Yin, K., & Neubig, G. (2022). Interpreting Language Models with Contrastive Explanations. Proceedings of the 2022 Conference on Empirical Methods in Natural Language Processing.







post-hoc

intrinsic



post-hoc

Interpretability is considered after the model is trained.

Leave-one-out, Gradient-based

intrinsic



post-hoc

Interpretability is considered after the model is trained.

Leave-one-out, Gradient-based

intrinsic

Models are architecturally constrained to be explained.

Attention, Decision Trees



post-hoc

Interpretability is considered after the model is trained.

intrinsic

Models are architecturally constrained to be explained.

Only models designed to be explained can be explained.

post-hoc

intrinsic

Models are architecturally constrained to be explained.

Only models designed to be explained can be explained.

post-hoc

intrinsic

Models are architecturally constrained to be explained.

Only models designed to be explained can be explained.

Intrinsic models can have high-performance too.

post-hoc

Interpretability is considered after the model is trained.

Black-box models are more general purpose.

intrinsic

post-hoc

Interpretability is considered after the model is trained.

Any model can be explained.

Black-box models are more general purpose.

intrinsic

The evolution of paradigms

Light is a particle.

Light is a wave.



The evolution of paradigms

Light is a particle.

Quantum mechanisms

Light is a wave.



post-hoc

Black-box models are more general purpose.

intrinsic

Only models designed to be explained can be explained.



New Interpretability Paradigms

Black-box models are more general purpose.

Only models designed to be explained can be explained.



Al Interpretability Needs a New Paradigm

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Siva Reddy^{†‡} siva.reddy@mila.quebec Mila Montréal, Quebec, Canada

Abstract Interpretability is the study of explaining models in understandable terms to humans. At present, interpretability is divided into two paradigms: the intrinsic paradigm, which believes that only models designed to be explained can be explained, and the post-hoc paradigm, which believes that black-box models can be explained. At the core of this debate is how each paradigm ensures its explanations are *faithful*, i.e., true to the model's behavior. This is important, as false but convincing explanations lead to unsupported confidence in artificial intelligence (AI), which can be dangerous. This article's perspective is that we should think about new paradigms while staying vigilant regarding faithfulness. First, by examining the history of paradigms in science, we see that paradigms are constantly evolving. Then, by examining the current paradigms, we can understand their underlying beliefs, the value they bring, and their limitations. Finally, this article presents 3 emerging paradigms for interpretability. The first paradigm designs models such that faithfulness can be easily measured. Another optimizes models such that explanations become faithful. The last paradigm proposes to develop models that produce both a prediction and an explanation.

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Keywords

Interpretability, Explanations, Transparency, Paradigms, Post-hoc, Intrinsic, Ethics, Future work, Faithfulness measurable models, Selfexplanations, Self-explaining models

ACM Reference Format:

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1 Introduction

There was a time in physics, in the late 17th century, when Isaac Newton insisted that light is a particle and Christiaan Huygens insisted that light is a wave. These ideas were seemingly irreconcilable at the time. Of course, now we have a much better theory, and we understand that light can be seen as both a wave and a particle.¹

In 1874, Georg Cantor proposed set theory and showed there exists at least two kinds of infinity. This divided the mathematical field. The Intuitionists, who named Cantor's theory nonsense, thought that math was a pure creation of the mind and that these infinities



How to provide and ensure faithful explanations for complex general-purpose neural NLP models? Research question

This question can be answered:

- explained without employing architectural constraints.
- notoriously troubling history regarding faithfulness.
- and NLP models.

By developing new paradigms that design models to be

By focusing on developing accurate faithfulness metrics.

By focusing on **importance measures** that have had a

By taking advantage of properties specific to natural language

Research hypothesis



Faithfulness measurable models

Model is designed such that measuring faithfulness is easy.

> ICML 2024 Spotlight

Potential paradigms

Self-explanations

Model is designed such that it can explain itself.

ACL 2024 Findings



Faithfulness measurable models

Faithfulness measurable model

80% faithful





model

The movie was great . I really liked it . *regular input*



erasure-metric

If a token is truly important, then if the token is removed, the model's prediction should change significantly.

Samek, W., et al. Evaluating the Visualization of What a Deep Neural Network Has Learned. *IEEE 2017.*

Hooker, S., Erhan, D., Kindermans, P.-J. J., & Kim, B. A benchmark for interpretability methods in deep neural networks. NeurIPS 2019.



Evaluating the Faithfulness of Importance Measures in NLP by Recursively Masking Allegedly Important Tokens and Retraining

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Abstract

To explain NLP models a popular approach is to use importance measures, such as attention, which inform input tokens are important for making a prediction. However, an open question is how well these explanations accurately reflect a model's logic, a property called *faithfulness*.

To answer this question, we propose Recursive ROAR, a new faithfulness matric. This works by recursively masking alleged in puttant tokens and then retraining the model. The principle is that this should result in worse model performance compared to masking random tokens. The result is a performance curve given a masking-ratio. Furthermore, we propose a summarizing metric using relative area-between-curves (RACU), which allows for easy comparison across papers, models, and tasks.

We evaluate 4 different importance measures on 8 different datasets, using both LSTMattention models and RoBERTa models. We find that the faithfulness of importance measures is both model-dependent and taskare relevant for a given prediction. This type of explanation is called an importance measure.

A major challenge in the field of interpretability is ensuring that an explanation is *faithful*: "a faithful interpretation is one that accurately represents the reasoning process behind the model's prediction" (Jacovi and Goldberg, 2020). Unfortunately, importance measures that are claimed to have strong theoretical foundations and are widely Discontrophatt et al., 2019) often later turn out to be predictionable (Hooker et al., 2019; Kinder-

mans et al., 2019; Adebayo et al., 2018; Jain and Walkay 2019; Wiegreffe and Pinter, 2019). Actuately measuring if an explanation is faith

Actuately measuring if an explanation is faithful is therefore paramount. Such *faithfulness* metrics are difficult to develop as the models are too complex to know what the correct explanation is. Doshi-Velez and Kim (2017) says a *faithfulness* metric should use "some formal definition of interpretability as a proxy for explanation quality."

In this work, we use the definition of *faithfulness* by Samek et al. (2017) and Hooker et al. (2019): if information (input tokens) is truly important, then



 $\mathsf{R}($

Compute importance measure Repeat this:

- 1. Mask 10% more of the dataset
- 2. Retrain the model
- 3. Measure the performance

0%	The	movie	was	great	I		really	liked
10%	The	movie	was	[[]]	I		really	liked



Explanation
Importance Measure





Compute importance measure Repeat this:





Explanation Importance Measure


Repeat this:



Explanation















Model and task-dependent faithfulness

	LSTM	RoBE
bAbl-1	59.1%	48.2
bAbl-2	34.6%	42.0
bAbl-3	25.9%	-27.9
Anemia	4.9%	12.5
Diabetes	11.4%	26.1
SST	37.8%	32.9
SNLI	-13.9%	56.7
IMDB	32.5%	35.1

Absolute Integrated Gradient



Same conclusion in: Bastings, J., et al. "Will You Find These Shortcuts?" A Protocol for Evaluating the Faithfulness of Input Salience Methods for Text Classification. EMNLP 2022



Limitations

- Computationally expensive:
 - Retrain the model 10 times
 - Importance measure on training dataset
 - For each: explanation, model, and dataset



Limitations

- Computationally expensive:
 - Retrain the model 10 times
 - Importance measure on training dataset
 - For each: explanation, model, and dataset
- Does not measure on the deployed model



Limitations

All because of retraining

Computationally expensive:
Retrain the model 10 times
Importance measure on training dataset
For each: explanation, model, and dataset
Does not measure on the deployed model
Leaks the classification target



What if we had a model that supported masking from the beginning?



Andreas Madsen¹² Siva Reddy¹³⁴ Sarath Chandar¹²⁵

Abstract

A common approach to explaining NLP models is to use importance measures that express which tokens are important for a prediction. Unfortunately, such explanations are often wrong despite being persuasive. Therefore, it is essential to measure their faithfulness. One such metric is if tokens are truly important, then masking them should result in worse model performance. However, token masking introduces out of-distribution issues, and existing solutions that address this are computationally expensive a employ proxy models. Furthermore, other metrics are very limited in scope. This work propose an inherently faithfulness measurable model th addresses these challenges. This is achieved using a novel fine-tuning method that incorporates masking, such that masking tokens become indistribution by design. This differs from existing approaches, which are completely model-agnostic but are inapplicable in practice. We demonstrate the generality of our approach by applying it to 16 different datasets and validate it using statistical in-distribution tests. The faithfulness is then measured with 9 different importance measures. Because masking is in-distribution, importance

1. Introduction

As machine learning models are increasingly being deployed, the demand for interpretability to ensure safe operation increases (Doshi-Velez & Kim, 2017). In NLP, importance measures such as attention or integrated gradient are a popular way of explaining which input tokens are important for making a prediction (Bhatt et al., 2019). These explanations are not only used directly to explain models but are also used in other explanations such as contrastive (Yin & Neubig, 2022), counterfactuals (Ross et al., 2021), adapted alternations (Ebrahimi et al., 2018).

Childraftely, importance measures (IMs) are often found to provide false explanations despite being persuasive (Jain Contract, 2019; Hooker et al., 2019). For example, a given in a might not be better at revealing important tokens than pointing at random tokens (Madsen et al., 2022a). This presents a risk, as false but persuasive explanations can lead to unsupported confidence in a model. Therefore, it's important to measure faithfulness. Jacovi & Goldberg (2020) defines faithfulness as: "how accurately it (explanation) reflects the true reasoning process of the model". In this work, we propose a methodology that enables existing models to support measuring faithfulness by design.

Measuring faithfulness is challenging, as there is generally no known ground-truth for the correct explanation. Instead, faithfulness metrics have to use provies. One such provy



Masked Language Models

• Pre-trained with 12% masking (RoBERTa)

• Catastrophic forgetting when fine-tuning



$$\mathscr{L}\left(X_{1:B}, y_{1:B}\right) = \widetilde{\mathscr{L}}\left(X_{1:\frac{B}{2}}, y_{1:\frac{B}{2}}\right) + \widetilde{\mathscr{L}}\left(mask\left(X_{\frac{B}{2}:B}\right), y_{\frac{B}{2}:B}\right)$$

Uniform masking: In half of the mini-batch. For each training observation:

- 1. Sample a masking ratio between 0% and 100%.
- 2. Mask random ratio% tokens in an observation.

Masked fine-tuning



41

0% masked performance



- Default hyperparameters.
- 95% confidence interval of the mean, 5 seeds.

42



- Default hyperparameters.
- 95% confidence interval of the mean, 5 seeds.





- Default hyperparameters.
- 95% confidence interval of the mean, 5 seeds.





Туре	Dataset
	RTE
	SNLI
	MNLI
	CB
Derebraa	MRPC
Parantase	QQP
Contimont	SST2
Sentiment	IMDB
Diagnacia	Anemia
Diagnosis	Diabetese
Acceptability	CoLA
	BoolQ
QA	bAbl-1
	bAbl-2
	bAbl-3



0% masked performance









0%





masking-ratio

47

- Should assume little of the model's internals. For example, do not assume internally normally distributed.
- Should only consider the model, not the input distribution.
- Should provide non-ambiguous metrics.



- Should assume little of the model's internals. For example, do not assume internally normally distributed.
- Should only consider the model, not the input distribution.
- Should provide non-ambiguous metrics.

[1] Matan, H., Frostig, T., Heller, R., & Soudry, D. A Statistical Framework for Efficient Out of Distribution Detection in Deep Neural Networks. ICLR 2022

- Use MaSF [1], a non-parametric statistical global in-distribution test.
- Originally made for small scale computer vision, which we adapt to large scale NLP.







 Because random masking is different form targeted masking, each explanation need to be tested.





OOD

- Because random masking is different form targeted masking, each explanation need to be tested.
- Often out-of-distribution issues with plain fine-tuning.



Masking ratio



- Because random masking is different form targeted masking, each explanation need to be tested.
- Often out-of-distribution issues with plain fine-tuning.
- No out-of-distribution issues with masked fine-tuning.



Masking ratio







Occlusion-based



51

Gradient-based

$$e(x_i) = \frac{\partial f(x)_c}{\partial x_i}$$
 The movie was g





Importance Measures







Masking ratio







Masking ratio



Dataset	IM	FMM	R-RO
SST2	Grad (L2)	40.4%	26.1
	X ⊙ grad (abs)	23.5%	18.6
	IG (abs)	45.3%	32.9
bAbl-2	Grad (L2)	96.3%	57.8
	X ⊙ grad (abs)	92.0%	48.1
	IG (abs)	98.3%	42.0

RoBERTa-Base

Comparison





Higher faithfulness

Dataset	IM	FMM	R-RO
SST2	Grad (L2)	40.4%	26.1
	X ⊙ grad (abs)	23.5%	18.6
	IG (abs)	45.3%	32.9
bAbl-2	Grad (L2)	96.3%	57.8
	X ⊙ grad (abs)	92.0%	48.1
	IG (abs)	98.3%	42.0

RoBERTa-Base

AR

- %
- \$%
-)%
- 8%
- %
-)%

John went to the office. Mary went to the hallway. John went to the bathroom.

Where is John?



Higher faithfulness

Dataset	IM	FMM	R-RO
SST2	Grad (L2)	40.4%	26.1
	X ⊙ grad (abs)	23.5%	18.6
	IG (abs)	45.3%	32.9
bAbl-2	Grad (L2)	96.3%	57.8
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	IG (abs)	98.3%	42.0

RoBERTa-Base

AR

- %
- \$%
- %
- %
- %
- %

[M] went [M] [M] [M]. [M] [M] to [M] [M]. John [M] to [M] bathroom.

- Produces a more robust model, that depends on more relevant signals.
- Faithful explanations then reveals objectively important information.



Not model and task-dependent

Dataset	IM	FMM	R-RO
bAbl-1	IG (abs)	93.7%	48.2
bAbl-2		98.3%	42.0
bAbl-3		100 %	-27.9
Anemia	IG (abs)	52.1%	12.5
Diabetes		90.5%	26.1
SST	IG (abs)	45.3%	32.9
SNLI		92.3%	56.7
IMDB		35.4%	35.1

RoBERTa-Base

AR

- %
- %
- 9%
- %
- %
- %
- %
- %

- Improvements across all datasets.
- There are now consistently good importance measures, across all 16 datasets.



Faithfulness measurable model

80% faithful





model

The movie was great . I really liked it . *regular input*



Optimizing for faithfulness

- Building on existing work which uses a beam-search optimizer [1].
- Slightly different faithfulness metric. They use but same idea.

[1] Zhou, Y., & Shah, J. The Solvability of Interpretability Evaluation Metrics. EACL Findings, 2023.

comprehensiveness – sufficiency, we use Recursive ROAR,

They do not address the OOD issues caused by masking.



Optimizing for faithfulness







Optimizing for faithfulness










Faithfulness



Masking ratio

Beam is not always optimal, because it's an approximation.







Summary

2. In-distribution validation

3. Measure faithfulness



Faithfulness Measurable Models

Black-box models are more general purpose.

Only models designed to be explained can be explained.



	less informa	tion	more information				
	post-hoc					intrinsic	
local explanation	black-box	dataset	gradient	embeddings	white-box	model specific	
input features	Occlusion -based §2.5.2		Gradient -based §2.5.1			$\begin{array}{c} \text{Attenton} \\ \text{-based } \S 2.5.3 \end{array}$	
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natural language	predict-then- explain ^{\mathcal{M}} § 2.7.2					explain-then- predict ^{\mathcal{M}} § 2.7.1	
class explanation							
concepts					$\operatorname{NIE}^{\mathcal{D}}$ § A.3.1		
global explanation							
vocabulary							
ensemble	SP-LIM	P-LIME § A.5.1					
linguistic information	Behavioral $\operatorname{Probes}^{\mathcal{D}}$ § A.6.1			Structural Probes ^{\mathcal{D}} §A.6.2	Structural Probes ^{\mathcal{D}} § A.6.2	$\begin{array}{c} \text{Auxiliary} \\ \text{Task}^{\mathcal{D}} \end{array}$	
rules	$\mathrm{SEAR}^{\mathcal{A}}$	¹ §A.7.1 Compos	sitional Explana	ations of Neurons ^{\dagger}	§A.7.2		



		less informat	tion	more information			
		post-hoc					intrinsic
lc	ocal explanation	black-box	dataset	gradient	embeddings	white-box	model specific
lower	input features	Occlusion -based §2.5.2		Gradient -based $\S2.5.1$			$\begin{array}{c} \text{Attenton} \\ \text{-based } \S 2.5.3 \end{array}$
abstra	adversarial examples	$SEA^{\mathcal{M}}$ §A.1.2		HotFl	ip §A.1.1		
ction	influential examples		Influence I Tra	Functions ^{\mathcal{H}} § A.2.1 cIn ^{\mathcal{C}} § A.2.3	Representer Poin	$ters^{\dagger}$ § A.2.2	Prototype Networks
	counter- factuals	$\begin{array}{c} \text{Polyjuice}^{\mathcal{M},\mathcal{D}} \\ \$ 2.6.1 \end{array}$	$MiCE^{\mathcal{M}}$ § 2.	6.2			
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glo	obal explanation						
hi	vocabulary				Project §A.4.1, Rotate §A.4.2		
oher al	ensemble	SP-LIM	E§A.5.1				
ostracti	linguistic information	Behavioral $\operatorname{Probes}^{\mathcal{D}}$ § A.6.1			$\begin{array}{c} \text{Structural} \\ \text{Probes}^{\mathcal{D}} \ \$ \text{A.6.2} \end{array}$	Structural Probes ^{\mathcal{D}} § A.6.2	$\begin{array}{c} \text{Auxiliary} \\ \text{Task}^{\mathcal{D}} \end{array}$
on	rules	$\mathrm{SEAR}^\mathcal{N}$	¹ § A.7.1 Con	mpositional Explan	ations of Neurons ^{\dagger}	§A.7.2	





F



LLMs are high-stakes decision makers

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Solution of the second seco

Is the following a good candidate for a Senior SWE position? Answer yes/no.

Resume:

 \equiv

Experience:

2017: Software Internship at Company X 2020-2023: Frontend SWE at a Medical Company Education:

2016-2020: Bachelor in Biology at University Y

No, this candidate may not be a good fit for a senior software engineer position. While they have some experience as a frontend software engineer and a background in biology, they lack extensive experience in software development, leadership roles, or technical expertise to qualify for a senior role. A senior software engineer typically requires more than 5 years of experience in software development, proven leadership

😉 huggingface.co/chat/conversation/65d666 🔒 🚥



F



Are self-explanations from Large Language Models faithful?

Sarath Chandar^{1,2,4} Andreas Madsen^{1,2} Siva Reddy^{1,3,5} ⁴ Canada CIFAR AI Chair ⁵ Facebook CIFAR AI Chair {firstname.lastname}@mila.quebec

¹ Mila – Quebec AI Institute ² Polytechnique Montréal ³ McGill University

Abstract

Instruction-tuned Large Language Models (LLMs) excel at many tasks and will dence in LLMs, thus increasing risk. Therefore it's important to measure if self-explanation truly reflect the model's behavior. Such a mean sure is called interpretability-faithfulness and in Oings is inaccessible, and many LLMs only have an inference API. To address this, we propose faithfulness. For example, if an LLM says a

2024

Model response









Cons

- Explanation is also produced by a black-box.
- Hard to measure faithfulness of free-formed explanations.





Cons

- Explanation is also produced by a black-box.
- Hard to measure faithfulness of free-formed explanations.

Pros

 The explanation could have greater access to the predictionmodel behavior.





Problem

Hard to measure faithfulness of free-formed explanations.



Problem

Hard to measure faithfulness of free-formed explanations.

Solution

Look at a subset of self-explanations which we know how to validate.



Session 1 (prediction and explanation)

What is the sentiment of the following paragraph? Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I liked this the movie, it was great.

Positive.



Session 1 (prediction and explanation)

What is the sentiment of the following paragraph? Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I liked this the movie, it was great.

Positive.

Edit the paragraph such that the sentiment is "negative". Make as few edits as possible.

I disliked this the movie, it was awful.



Session 1 (prediction and explanation)

What is the sentiment of the following paragraph? Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I liked this the movie, it was great.

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Edit the paragraph such that the sentiment is "negative". Make as few edits as possible.

I disliked this the movie, it was awful.





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Edit the paragraph such that the sentiment is "negative". Make as few edits as possible.

I disliked this the movie, it was awful.

Session 2 (Self-consistency)

What is the sentiment of the following paragraph? Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I disliked this the movie, it was awful.



-992

Negative



Session 1 (prediction and explanation)

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What is the sentiment of the following paragraph? Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I disliked this the movie, it was awful.



Negative



Sentiment feature attribution

Session 1 (prediction and explanation)

What is the sentiment of the following paragraph? The paragraph can contain redacted words marked with [REDACTED]. Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I liked this the movie, it was great.



Important words: "liked," "great".

Session 2 (Self-consistency)

What is the sentiment of the following paragraph? The paragraph can contain redacted words marked with [REDACTED]. Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I [REDACTED] this the movie, it was [REDACTED].



Sentiment redaction

Session 1 (prediction and explanation)

What is the sentiment of the following paragraph? The paragraph can contain redacted words marked with [REDACTED]. Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I liked this the movie, it was great.

No

Redact the most important words for determining the sentiment, by replacing important words with [REDACTED], such that without these words the sentiment can not be determined.

Paragraph: I [REDACTED] this the movie, it was [REDACTED].





Session 2 (Self-consistency)

What is the sentiment of the following paragraph? The paragraph can contain redacted words marked with [REDACTED]. Answer only "positive", "negative", "neutral", or "unknown":

Paragraph: I [REDACTED] this the movie, it was [REDACTED].

Direct redaction



The movie was great.



The movie was great.

Session 1

Classification prompt.

Positive



Session 1

Classification prompt.

Positive

Counterfactual explanation prompt.

The movie was awful.

explanation prompt.









The movie was awful.

Session 2

Session 1

Classification prompt.

Negative



Unknown







Classification





Classification



Because the goal is not a high accuracy LLM classifier, we just discard misclassified observations.









Model-dependent.

Model-dependent.

• Task-dependent.

100% -75% - • 50% -25% -0% -100% -75% -50% -25% -0% -100% -75% -50% -25% -0% -

Faithfulness



- Model-dependent.
- Task-dependent.
- Explanation-dependent.



- Model-dependent.
- Task-dependent.
- Explanation-dependent.

In general, we can't trust LLMs' self-explanations.









Robustness

What about prompt variations?



Redaction instruction

If the model was generally faithful but one prompt variation was not, that would be problematic.

Robustness



If the model was generally faithful but one prompt variation was not, that would be problematic.

Robustness


How can we make LLMs' self-explanations faithful?





What are we aligning towards

Human preference.



What are we aligning towards

Humans don't know how the model behaves.

Human preference.



What are we aligning towards

Humans don't know how the model behaves.



Fairwashing

Case 1

Is the following candidate a good fit for a Senior SWE position? Answer only yes/no.

Education: 2016-2020: Bachelor in Biology at University Y

Extra: Member of <u>Women's</u> Chess Club

No, the education does not match the position.

[1] Aïvodji, U., Arai, H., Fortineau, O., Gambs, S., Hara, S., & Tapp, A. Fairwashing: The risk of rationalization. ICML 2019

Case 2

Is the following candidate a good fit for a Senior SWE position? Answer only yes/no.

Education: 2016-2020: Bachelor in Biology at University Y

Extra: Member of Chess Club

Yes.

[2] Aïvodji, U., Arai, H., Gambs, S., & Hara, S. Characterizing the risk of fairwashing, NeurIPS 2021.



Fairwashing

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Case 2

Is the following candidate a good fit for a Senior SWE position? Answer only yes/no.

Education: 2016-2020: Bachelor in Biology at University Y

Extra: Member of Women's Chess Club

No, because it's a women.



[2] Aïvodji, U., Arai, H., Gambs, S., & Hara, S. Characterizing the risk of fairwashing, NeurIPS 2021.







Self-explanations

Black-box models are more general purpose.

Only models designed to be explained can be explained.



Self-explanations

Optimize also for faithfulness

Self-modeling capabilities

More faithfulness metrics









Conclusion

How to provide and ensure faithful explanations for complex general-purpose neural NLP models? Research question

This question can be answered:

- explained without employing architectural constraints.
- notoriously troubling history regarding faithfulness.
- and NLP models.

By developing new paradigms that design models to be

By focusing on developing accurate faithfulness metrics.

By focusing on **importance measures** that have had a

By taking advantage of properties specific to natural language

Research hypothesis



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Model and task-dependent faithfulness

- The faithfulness of post-hoc and attention is model and task-dependent.
- Shown on importance measures and selfexplanations. Simultaneously works [1,2] with same conclusion.

Same conclusion in: [1] Bastings, J., et al. "Will You Find These Shortcuts?" A Protocol for Evaluating the Faithfulness of Input Salience Methods for Text Classification. EMNLP 2022

Evaluating the Faithfulness of Importance Measures in NLP by Recursively Masking Allegedly Important Tokens and Retraining

Andreas Madsen^{1,2} Nicholas Meade^{1,3,*} Vaibhav Adlakha^{1,3,*} Siva Reddy^{1,3,4} ¹ Mila – Quebec AI Institute ² Polytechnique Montréal ³ McGill University ⁴ Facebook CIFAR AI Chair {firstname.lastname}@mila.quebec

Abstract

To explain NLP models a popular approach is which inform input tokens are important for making a prediction. However, an open question is how well these explanations accurately reflect a model's logic, a property called faith-

model performance compared to masking random tokens. The estilit is performance Wallace, 2019, Ruebayo et al., 2019, Ruebayo et al.,

We evaluate 4 different importance measure on 8 different datasets, using both LSTMattention models and RoBERTa models. We sures is both model-dependent and taskous evaluations in both computer vision and are relevant for a given prediction. This type of explanation is called an importance measure.

A major challenge in the field of interpretability is ensuring that an explanation is *faithful*: "a faithful interpretation is one that accurately represents the reasoning process behind the model's prediction" (Jacovi and Goldberg, 2020). Unforwe the first of the project of the strong st

pretability as a proxy for explanation quality."

In this work, we use the definition of *faithfulness* by Samek et al. (2017) and Hooker et al. (2019): if information (input tokens) is truly important, then removing it should result in a worse model performance compared to removing random information (tokens). We build upon the ROAR metric by

Are self-explanations from Large Language Models faithful?

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[2] Lanham, T., et al. Measuring Faithfulness in Chain-of-Thought Reasoning. Pre-print 2023.

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- Shown on importance measures and selfexplanations. Simultaneously works [1,2] with same conclusion.
- Likely to explain why there is so much debate on is X-method faithful.
- Only revealed using sufficiently accurate faithfulness metric at large scope.

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Consistent faithfulness

Recursive ROAR

Model and task-dependent

Faithfulness Measurable Models

Masked fine-tuning creates consistently faithful explanations.

Self-explanations faithfulness metric

Explanation, model and task-dependent

Faithfulness as a reward function

 \mathcal{O}

How to provide and ensure faithful explanations for complex general-purpose neural NLP models? Research guestion

This question can be answered:

- By developing new paradigms that design models to be explained without employing architectural constraints.
- By focusing on developing accurate faithfulness metrics.
- By focusing on importance measures that have had a notoriously troubling history regarding faithfulness.
- By taking advantage of properties specific to natural language and NLP models.

Research hypothesis



New Interpretability Paradigms

Faithfulness measurable models

Model is designed such that measuring faithfulness is easy.

Black-box models are more general purpose.

Self-explanations

Model is designed such that it can explain itself.

Only models designed to be explained can be explained.





- The faithfulness of post-hoc methods is model and task-dependent.
- Yes, It's possible to develop new interpretability paradigms, which show consistent faithfulness.

Conclusion

Post-hoc Interpretability for Neural NLP: A Survey



Evaluating the Faithfulness of Importance Measures in NLP by **Recursively Masking Allegedly Important Tokens and Retraining**

Andreas Madsen^{1,2} Nicholas Meade^{1,3,*} Vaibhav Adlakha^{1,3,*} Mila – Quebec AI Institute ² Polytechnique Montréal ³ McGill University ⁴ Facebook CIFAR AI Chair {firstname.lastname}@mila.quebec

Abstract

on 8 different datasets, using both LSTM

file Received is logic, a property called faith prediction Ray and Cold Arg. The second state of the secon inc<u>ple is</u> Au that shall result in worse ode performane compart to masking ran-m action we result is a performance. The formation of the performane state of the performance of the pe

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Abstract	
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inference API. To address this, we propose employing self-consistency checks to master faithfulness. For example, if an LLM safe a set of words is important for making a <u>director</u> tion, then it should not be able to make its)24

AI Interpretability Needs a New Paradigm

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Siva Reddy^{†‡} siva.reddy@mila.quebec Mila Montréal, Quebec, Canada

s. So part, interpretability & duridal into two trinkic participantic biever at any models with the back over the state of e dangerous. This article's put to plan in this put to plan in this put to plan in the pla

CCS Concepts

 $\bullet \ \textbf{Computing methodologies} \rightarrow \textbf{Neural networks}; \textit{Natural landary} \\$ guage processing; • Human-centered computing \rightarrow Interaction paradigms; • Social and professional topics \rightarrow Governmental

Harvard University Cambridge, Massachusetts, United State Sarath Chandar*

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that math was a pure creation of the mind and that these infinities weren't real. Henri Poincaré said: "Later generations will regard

The other group, the Formalists, thought that by using Cantor set theory, all math could be proven from this fundamental founda

in Finder of the second se

Measurable Models to unsupported optional parameters of the model. In the option of the model of the

Faithfulness Measurable Masked Language Models

we can optimize explanations towards maximal faithfulness; thus, our model becomes indirectly

hfulness is challenging, as there is generally nd-truth for the correct explanation. Instead, etrics have to use proxies. One such proxy



ons JS

Pitfalls and Principles

Principles

The two options for measuring faithfulness:a) Use an intervention, but avoid out-of-distribution issues.b) Use a ground truth, but make sure it's an actual ground truth.

Pitfalls

- a) If correlating, it must be done with a known faithful explanation (which likely doesn't exist).
- b) Don't assume the model is reasonable (or accurate?).
- c) Don't assume you know what correct explanation looks like (follows previous).
- d) Don't mutate the internals of a model to validate explanation, you may escape the manifold.
- e) Don't probe the model behavior with out-of-distribution data.
- f) Don't use a different model to comment about the original model, unless the model behavior is identical.
- g) Don't assume faithfulness generalize to other datasets or models without validation. h) Not declaring what faithfulness measures. For example, gradient is faithful it is just
- not a measure of importance.
- Thinking there is just one correct explanation (importance measure) without a mathematical proof of uniqueness.

Explanation-interpretation gap

Mathematical/axiomatic faithfulness metric.

e.g. "How good is the gradient approximation?", "are they Sharply values?"

Explanation-interpretation gap

Faithfulness metric that reflects how we communicate explanations to humans.

e.g. "Without this token the model prediction changes significantly"









Interference error Approximation error Explanation-interpretation gap + leakage error

Approximations Actual issues

Mathematical/axiomatic faithfulness metric.

e.g. $\mathbf{x} \odot \nabla_{\mathbf{x}} f(\mathbf{x})$

e.g. Sharply approximation. e.g. "How good is the gradient approximation?", "are they Sharply values?"

All the gaps

Faithfulness metric that reflects how we communicate explanations to humans.

e.g. "Without this token the model prediction changes significantly"







		less informa	tion			me	ore information
		post-hoc					intrinsic
	local explanation	black-box	dataset	gradient	embeddings	white-box	model specific
lower	input features	Occlusion -based §2.5.2		Gradient -based $\S2.5.1$			Attenton -based §2.5.3
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on	rules	$\mathrm{SEAR}^{\mathcal{N}}$	^{1} §A.7.1 Compo	sitional Explana	tions of Neurons [†]	§A.7.2	

Local Explanation

		$p(y \mathbf{x})$	y	c
X	the year 's best and most unpredictable comedy	0.91	1	1
x	we never feel anything for these characters	0.95	0	0
\mathbf{X}	handsome but unfulfilling suspense drama	0.18	0	1

Which tokens are most important for the prediction?

Input features

Adversarial examples

Local Explanation

	$p(y \mathbf{x})$	y
x the year 's best and most unpredictable comedy	0.91	1
the year 's finest and most unpredictable comedy	0.30	_
$ ilde{ extbf{x}}$ the year 's finest and most unforeseeable comedy	0.08	_
x we never feel anything for these characters	0.95	0
$ ilde{\mathbf{x}}$ we never feel anything for these people	0.03	-

What would break the model's prediction?

Influential examples

Local Explanation

 \mathbf{X}

- x the year 's best and most un
- $\tilde{\mathbf{x}}$ a delightfully unpredictable
- $\tilde{\mathbf{x}}$ loud and thoroughl

What training examples influenced the prediction?

	$p(y \mathbf{x})$	y	Δ
predictable comedy	0.91	1	_
, hilarious comedy	0.95	1	3.82
y obnoxious comedy	0.98	0	-1.51



Local Explanation



Counterfactuals

	$p(y \mathbf{x})$	y
predictable comedy	0.91	1
predictable comedy	0.59	_
♥ predictable comedy	0.04	_
r these characters	0.95	0
r these characters	0.73	_
for these animals	0.01	_

What does the model consider a valid opposite example?

Local Explanation

 \mathbf{X}

0.91 1 the year 's best and most unpredictable comedy \mathbf{X} unpredictable comedies are funny —

0.95 0 we never feel anything for these characters \mathbf{X}

> it is important to feel for characters —

What would a generated natural language explanation be?

Natural Language

p(y	$ \mathbf{x})$	y





What concepts (e.g. occupations) can explain a class?

Concepts

Class Explanation



Global Explanation



How does the model relate words to each other?

Vocabulary

Ensamble

Global Explanation



What examples are representative of the model?
Linguistic information Global Explanation



What linguistic information does the model use?

	$p(y \mathbf{x})$	y	Flips
\mathbf{x} the year 's best and most unpredictable comedy	0.91	1	—
$\tilde{x} \ \texttt{the} \ \texttt{best} \ \texttt{and} \ \texttt{most} \ \texttt{unpredictable} \ \texttt{comedy} \ \texttt{this} \ \texttt{year}$	0.13	_	_
rule \underline{DET} year $\underline{'s} \rightarrow \underline{this}$ year	_	_	1 $\%$
x we never feel anything for these characters	0.95	0	—
$ ilde{\mathbf{x}}$ we never empatize for these characters	0.11	_	—
rule $\underline{feel} \rightarrow \underline{empatize}$	_	_	4 %

Which general rules can summarize an aspect of the model?

Rules

Global Explanation

		less information	tion			mo	ore inf
		post-hoc					intrin
	local explanation	black-box	dataset	gradient	embeddings	white-box	mod
lower	input features	Occlusion -based §2.5.2		Gradient -based §2.5.1			A -bas
abstra	adversarial examples	$SEA^{\mathcal{M}}$ §A.1.2		$HotFli_{j}$	р§А.1.1		
ction	$ \begin{array}{c} \text{influential} \\ \text{examples} \end{array} $		Influence Func TracIn ^C	$\begin{array}{l} \text{ctions}^{\mathcal{H}} \ \S \text{A.2.1} \\ \S \text{A.2.3} \end{array}$	Representer Poin	ters^{\dagger} § A.2.2	Pr N
	counter- factuals	$\begin{array}{c} \text{Polyjuice}^{\mathcal{M},\mathcal{D}} \\ \$ 2.6.1 \end{array}$	$MiCE^{\mathcal{M}}$ §2.6.2				
	natural language	predict-then- explain ^{\mathcal{M}} § 2.7.2					exp] predi
	class explanation						
	$\operatorname{concepts}$					$\operatorname{NIE}^{\mathcal{D}}$ §A.3.1	
	global explanation						
higher a	vocabulary				Project §A.4.1, Rotate §A.4.2		
	ensemble	SP-LIM	E § A.5.1				
ostracti	linguistic information	Behavioral $\operatorname{Probes}^{\mathcal{D}} \S A.6.1$			Structural Probes ^{\mathcal{D}} § A.6.2	Structural $\operatorname{Probes}^{\mathcal{D}} \S A.6.2$	A
on	rules	$\mathrm{SEAR}^{\mathcal{N}}$	¹ §A.7.1 Compo	sitional Explana	tions of Neurons [†]	§A.7.2	



• Most methods are not evaluated well, and there have been little improvement.

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		post-hoc					intrin
	local explanation	black-box	dataset	gradient	embeddings	white-box	mod
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	counter- factuals	$\begin{array}{c} \text{Polyjuice}^{\mathcal{M},\mathcal{D}} \\ \$ 2.6.1 \end{array}$	$MiCE^{\mathcal{M}}$ §2.6.2				
	natural language	predict-then- explain ^{\mathcal{M}} § 2.7.2					expl predi
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- Class explanation methods is lacking, especially compared to computer vision.

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- Class explanation methods is lacking, especially compared to computer vision.
- There is new work in computer vision that bridges the gap between *post-hoc* and *intrinsic*. Which is have not been adopted.

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- Class explanation methods is lacking, especially compared to computer vision.
- There is new work in computer vision that bridges the gap between *post-hoc* and *intrinsic*. Which is have not been adopted.
- Large Pre-trained models, like GPT-2 and T5, have enabled great progress in creating fluent explanations.

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Recursive-ROAR

Desirables

a) The method does not assume a known true explanation.

- and single observation. For example, it is not a proxy-model that is measured.
- c) The method uses only the original dataset, e.g. does not introduce spurious correlations.
- w.r.t. the model.
- computes explanations of the test dataset.
- The method can be applied to any classification task. **†**)
- g) The method can be applied to any importance measure.

Recursive ROAR: satisfies (a), (c), (d), (f), and (g).

b) The method measures faithfulness of an explanation w.r.t. a specific model instance

d) The method only uses inputs and intermediate representations that are in-distribution

e) The method is computationally cheap by not training/fine-tuning repeatedly and only

Leaking target variable

Thought experiment

- a) Say "awful" is a strong indicator of negative sentiment.
- b) Recursive ROAR will remove "awful" from every negative sentiment observation.
- c) "awful" is now a perfect predictor of positive sentiment. e.g. "I have an awful strong crush on this actor"

We want an importance measure for the correct label, as removing the tokens that are relevant for making a wrong prediction, would help the performance of the model.

Leaking target variable

- $\{x_1, x_2, x_3, x_4\}$ are relevant features, but mutually redundant. All other features are irrelevant to the target value.
- z, η, ϵ are sampled for each observation. r_i , s_i are sampled once. A standard normal distribution is used.
- The explanation is the weights of a logistic regression.

Test Accuracy 08,000

Juacy 100%

$$\mathbf{x} = \frac{\mathbf{a}z}{10} + \mathbf{d}\eta + \frac{\epsilon}{10}, \quad y = \begin{cases} 1 & z > 0\\ 0 & z \le 0 \end{cases}$$

- $a = [r_1, r_2, r_3, r_4, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]$
- $d = [s_1, s_2, s_3, s_4, s_5, s_6, s_7, s_8, s_9, s_{10}, s_{11}, s_{12}, s_{13}, s_{14}, s_{15}, s_{16}]$ $x = \left[\frac{r_{1}z}{10} + s_{1}\eta + \frac{\epsilon}{10}, \dots, \frac{r_{4}z}{10} + s_{4}\eta + \frac{\epsilon}{10}, s_{5}\eta + \frac{\epsilon}{10}, \dots, s_{16}\eta + \frac{\epsilon}{10}\right]$





Attention Models

single sequence to class

Tasks: SST, IMDB, Anemia, Diabetes



[1] Vashishth et al, arXiv 2019, "Attention Interpretability Across NLP Tasks" [2] dain, AGL 2019,0" Attention is not Explanation". ¹³95

paired sequence to class

Tasks: SNLI, bAbI-1, bAbI-2, bAbI-3



Papers on the faithfulness of attention

Paper	Compare with other importance measure	Test if mutated attention can yield same prediction	Test if learned adversarial attention can yield same prediciton.
Attention is not explanation (ACL 2019)	X	X	
Attention is not not explanation (EMNLP 2019)			Χ
Attention interpretability Across NLP Tasks (ArXiv 2019, ICLR 2020 Reject)		Χ	Χ
Is Attention Interpretable (ACL 2019)		X	
Learning to Deceive with Attention-Based Explanations (ACL 2020)			Χ
Is Sparse Attention more Interpretable (ACL 2021)	X	X	X
	Criticism: Other methods are not ground-truths.	Criticism: Mutating the attention causes out-out-distribution	Criticism: Learning a different models says nothing about the original

issues.











model.



No performance issues

0% masked performance



100% masked performance





In-distribution testing

- Because random masking is different form targeted masking, each explanation need to be tested.
- Often out-of-distribution issues with plain fine-tuning.
- No out-of-distribution issues with masked fine-tuning.







Masking ratio





Sequential output

Requirements are: 1) performance metric and 2) importance measure / ranking.

- 1. Performance Measure: ROUGE, BLEU, Levenstein.
- optimization, etc.

2. Importance measure: Leave-on-out, naive aggregation,



Learn masking support during pre-training Mask random tokens during pre-training with a next-token objective.

Masked CLMs

Learn masking support during pre-training Mask random tokens during pre-training with a next-token objective.

- 1. An Faithfulness Measurable model.
- 2. Get highly faithful occlusion-based importance measure.

Masked CLMs

























Learn masking support during pre-training Mask random tokens during pre-training with a next-token objective.

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- 3. Zero-cost parallel-token generation.

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Learn masking support during pre-training Mask random tokens during pre-training with a next-token objective.

- 1. An Faithfulness Measurable model.
- 2. Get highly faithful occlusion-based importance measure.
- 3. Zero-cost parallel-token generation.
- 4. Many established techniques from MLM.
- 5. Standard for how to anonymize data.



MaSF

Manifolds





Desirables

- not assume internally normally distributed.
- (sensory anomaly detection).
- Should provide non-ambiguous metrics.

• Should assume little of the model's internals. For example, do

Should only consider the model, not the input distribution
Empirical CDF





Empirical CDF







Empirical CDF



One-sided p-value $p = \mathbb{P}(X \le x)$ $\approx \frac{1}{|D|} \sum_{v \in D} \mathbb{1}[v \le x] \text{ where } D \sim X$

Two-sided p-value

 $p = \min(\mathbb{P}(X \le x), \mathbb{P}(X > x))$ $= \min(\mathbb{P}(X \le x), 1 - \mathbb{P}(X \le x))$





The movie was great. I really liked it.





















P-value aggregation

Bonferroni

Avoid p-fishing by dividing the threshold by N.



$$p_i < \frac{5\,\%}{N}$$

$$N \cdot \min_{i=1}^{N} p_i < 5\%$$

N mi i=1

wher

Simes

Consider all p-values. For the smallest p-value (i=1) it is the same.



No clear intuition. Follows a chi-squared distribution.

$$n_{1} \frac{p_{i} \cdot N}{i} < 5\%$$

$$P_{1} < p_{2} < \dots < 1$$

 p_N

$$T = -2\sum_{i=1}^{N}\ln(p_i)$$



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FMMs for other explanations

Concept explanations

- Faithfulness of concepts is often measured using interventions in the intermediate state.
- These intervention likely cause out-of-distribution issues.



Grevy's Zebra Stallion, CC BY-SA 2.0





Self-explanations

A model should be able to simulate itself, to explain itself in general.

Self-modeling

Self-modeling

Meta-cognition question

Are you able to answer who was the first president of the United States? Yes/No

No

Direct question

Who was the first president of the United States?

George Washington

How does this generalize?

Optimize for this





How does th

Optimize for this



	nis	genera)
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Evaluate on this



On Measuring Faithfulness of Natural Language Explanations

Abstract

Large language models (LLMs) can explain ever the LLM could make up reasonably soundcommon suite of 11 open-source LLMs and LLM self-consistency that compares a model's

Letitia Parcalabescu and Anette Frank **Computational Linguistics Department** Heidelberg University

tions even with irrelevant or misleading prompts

Even though LLMs can provide plausibly sounding Claims: currently no general faithfulness metric for for the true reasoning natural language explanations - whether it is AI uncovering new scientific facts or ChatGPT helping with homework.

LLM-produced NLEs through faithfulness tests (Atanasova et al., 2023; Turpin et al., 2023; Lan-



Integrated Gradient

Integrated Gradient axioms

Completeness

Attributions $\phi_i(x, f)$ for each feature i should sum to the total value f(x).

$$\sum_{i=1}^{n} \phi_i(x, f) = f(x)$$

Implementation Invariance

The attributions are always identical for two functionally equivalent networks.

Sensitivity

If for every input and baseline that differ in one feature but have different predictions, then the differing feature should have non-zero attribution.

Integrated Gradient axioms

where $f(\mathbf{x}; \theta)$ is the model logits.

- $\mathbf{E}_{\text{integrated-gradient}}(\mathbf{x}, c) = (\mathbf{x} \mathbf{b}) \odot \frac{1}{k} \sum_{i=1}^{k} \nabla_{\tilde{\mathbf{x}}_{i}} f(\tilde{\mathbf{x}}_{i}; \theta)_{c}, \quad \tilde{\mathbf{x}}_{i} = \mathbf{b} + \frac{i}{k} (\mathbf{x} \mathbf{b}),$



Shapely axioms

Efficiency / Completeness

Attributions $\phi_i(x, f)$ for each player *i* should sum to the total value f(x).

$$\sum_{i=1}^{n} \phi_i(x, f) = f(x)$$

Symmetry

If two players a and b are identical, they should receive equal attribution. $\phi_a(x,f) = \phi_b(x,f)$ if $f(S \cup \{a\}) = f(S \cup \{b\})$ $\forall S \subseteq x \setminus \{a, b\}$

Additivity / Linearity

If the value can be linearly decomposed a f + g, the attributions $\phi_i(x, f)$ can be decomposed too. $\phi_i(x, f+g) = \phi_i(x, f) + \phi_i(x, g)$

Null Player

Attribution for a player i who doesn't contribute is zero. $\phi_i(x, f) = 0$ $if f(S \cup \{i\}) = f(S)$ $\forall S \subseteq x \setminus \{i\}$

$\phi_i(x,f) = \sum_{i=1}^{n} \frac{|S|!(|x|)|}{|x|}$ $S \subseteq x \setminus \{i\}$

Shapely

$$\frac{|-|S|-1)!}{|x|!} \left(f(S \cup \{i\}) - f(S) \right)$$

- \$15 for Alice alone.
- Charlie lives further away, increases the cost to \$51.

Passengers	Cost
$\{\varnothing\}$	\$O
{Alice}	\$15
{Bob}	\$25
{Charlie}	\$38
{Alice, Bob}	\$25
{Alice, Charlie}	\$41
{Bob, Charlie}	\$51
{Alice, Bob, Charlie}	\$51



Alice and Bob live together, but Bob wants a luxurious tax, adding 10\$.

Note

- No taxi ride, no costs
- Standard fare to Alice's & Bob's place
- Bob always insists on luxury taxis
- Charlie lives slightly further away
- Bob always gets his way
- Drop off Alice first, then Charlie
- Drop off luxurious Bob first, then Charlie
- The full fare with all three of them

Shapely Example

1. Consider every order of Alice, Bob, Charlie.

- Alice, Bob, Charlie
- Alice, Charlie, Bob
- Bob, Alice, Charlie
- Charlie, Alice, Bob
- Bob, Charlie, Alice
- Charlie, Bob, Alice

Passengers	Cos
$\{\varnothing\}$	\$0
{Alice}	\$15
{Bob}	\$25
{Charlie}	\$38
{Alice, Bob}	\$25
{Alice, Charlie}	\$41
{Bob, Charlie}	\$51
{Alice, Bob, Charlie}	\$51



Shapely Example

1. Consider every order of Alice, Bob, Charlie.

2. Consider Alice is the last to enter the taxi.

- Alice, Bob, Charlie
- Alice, Charlie, Bob
- Bob, Alice, Charlie
- Charlie, Alice, Bob
- Bob, Charlie, Alice
- Charlie, Bob, Alice

Passengers	Cos
$\{\varnothing\}$	\$0
{Alice}	\$15
{Bob}	\$25
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{Alice, Bob}	\$25
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{Alice, Bob, Charlie}	\$51



Shapely Example

1. Consider every order of Alice, Bob, Charlie.

2. Consider Alice is the last to enter the taxi.

3. Average up Alice's contributions.

• Alice, Bob, Charlie • Alice, Charlie, Bob • Bob, Alice, Charlie • Charlie, Alice, Bob • Bob, Charlie, Alice • Charlie, Bob, Alice

 $\{\emptyset\} \rightarrow \{A | ice\} = \15 $\{\emptyset\} \rightarrow \{Alice\} = \15 $\{Bob\} \rightarrow \{Alice, Bob\} = \0 {Charlie} \rightarrow {Alice, Charlie} = \$3

Average: \$5.5

 $\{Bob, Charlie\} \rightarrow \{Alice, Bob, Charlie\} = \0 {Bob, Charlie} \rightarrow {Alice, Bob, Charlie} = \$0

Passengers	Cos
{Ø}	\$0
{Alice}	\$15
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Background / Baseline data



○ = Baseline Data ○ = Data Point to be explained

Feature

https://mindfulmodeler.substack.com/p/shedding-light-on-impossibility-theorems







Visualization



https://shap.readthedocs.io/en/latest/

